

AM-91-477

Pyroxene-garnet equilibration during cooling in the mantle

Douglas Smith, Barbara R. Barron

For deposit: Table 2

American Mineralogist, 76, 11-12, 1950-1963.

PROGRAM COOLV3a

C Adapted from Barron (1985, "Diffusion rate estimates

C from pyroxene, Garnet Ridge, Arizona", U. Texas Austin

C master's thesis)

C Modified by D. Smith - this version is of 6/15/90.

C Comments changed in 5/91 by DS

! Doug Smith (for program copy, send Mac disk)

! Department of Geological Sciences

! U. Texas Austin, Austin, TX 78713

! 512-452-7768

C The program simulates one-dimensional diffusion of Al

C in an orthopyroxene sphere included within garnet.

C This version sets the wt % Al₂O₃ at the opx surface by a

C polynomial fit to values calculated by the method of

C Harley (1984). The boundary condition is specific for

C the compositions of the opx and garnet in grain 1, GR1.

C A Crank-Nicholson subroutine is used.

C The program is a descendent of programs of Wilson and Smith

C written in FORTRAN4 to model Fe-Mg in olivine-garnet pairs.

C See Smith and Wilson, 1985, Amer Mineral 70, 30-39.

C This version has been adapted to take advantage of FORTRAN77 and

C some of the extensions available in Abssoft MacFortran.

C It runs on a MacPlus, MacSE, or MacII.

C NOT all options in this modified code have been tested!

C Some are simply retained from earlier versions.

REAL RATES(20), TZEROS(20)

REAL U(1000), UNEW(1000), X(1000)

REAL TFINALS(20)

REAL UINITL(11)

REAL WPCTAL,C(4) !C contains coefficients for Harley calc

INTEGER MM,DD,YY,SECONDS !used in date, time subs

CDescription of some variables.....

C U is the vector of concentration values, UNEW is the updated

C version, and x is the array of locations at which the

C concentrations are calculated. WPCTAL is the weight % Al₂O₃

C in the opx at the garnet contact.

C Data must be read in from the file COOLDA2

C Results are written into the files COOLOU and COOLPL

OPEN (UNIT=4,FILE='COOLDA2',STATUS='OLD') !Input

OPEN (UNIT=5,FILE='COOLOU',STATUS='NEW') ! output to read

OPEN (UNIT=6,FILE='COOLPL',STATUS='NEW') ! output for plot

RGAS=8.314

JJ=1

II=JJ

CONVERT=3600.*24.*365.25*1.0E12 !m²/sec to microns²/yr

TSURF=273.15

CALL DATE(MM,DD,YY) !External subS must be on disk

CALL TIME(SECONDS)

STARTTIME = SECONDS

```

5   FORMAT(/,1X,I2.2,2('I2.2),5X,A30,2X,A25) !For date
      WRITE (5,5) MM,DD,YY,'D Smith COOLV3 Harley, 6/15/90',
1   'for gar 1, GR1, 20 kb'
           ! MM,DD,YY from external sub DATE

```

C Read from file 4, titled COOLDA2

```
READ (4,*) NX !Number of X values (<1000)
```

```
READ (4,*) DX !X increment in micrometers
```

```
WRITE(5,*)"NX is ',NX,'    DX is ',DX
```

```
DO (I=1,NX)
     X(I)=DX*I
REPEAT
```

```
READ (4,*) DZERO !Pre-exp diffusivity in m2/sec
WRITE(5,*)"DZERO in meters2/sec is ',DZERO
DZERO=DZERO*CONVERT !to microns2/year
```

```
READ (4,*) H !Activation enthalpy for diffusion (j/m)
WRITE(5,*)"H, Activation Q for diffusion (joules)',H
```

```
READ (4,*) NMAX !Max # of steps in cooling
WRITE(5,*)"NMAX number of time steps = ',NMAX
```

```
! Limits for maximum and minimum time steps
READ (4,*) DTMIN,DTMAX !values in years
WRITE (5,*)"DTMIN = ',DTMIN,' DTMAX =',DTMAX,' YRS'
           !The size of the time step begins at DTMIN and
           ! is scaled upwards as the diffusivity increases
           ! but is never allowed to exceed DTMAX.
```

```
PRESSR = 20000 ! Pressure (units are bars)
!The Harley T-Al coefficients (array C) must be for this P *****
```

```
1   READ (4,*) TZERO !Starting T (K)
      WRITE(5,*)"TZERO starting T(deg K)',TZERO,
           ' at PRESSR P(bars)',PRESSR
```

```
READ (4,*) NT !Number of final temperatures (NT>1 not tested here)
WRITE (5,*)"Number of final temps is ',NT
```

```
NR = 1 !Number of cooling rates (NR>1 not tested here)
```

```
READ (4,*) LE !1 is linear, 0 cooling slab, -1 exponential
```

```
WRITE(5,*)"1, linear: 0, slab: -1, exp: LE = ',LE
```

```
READ (4,*) HOLDTIM !Years to hold if 0 or +
           !If negative, then total of cooling + holding
      WRITE(5,*)"HOLDTIM (if -, cooling + holding)',HOLDTIM
```

```
IF (LE.EQ.0) TSURF = 298 !Surface T for slab model
```

C*****Start do loop of multiple final temps and rates *****

! This code has been run only with 1 temp and rate.
DO 240 II=1,NT

! II counts the index of the final temperature

NR=1

! JJ counts the index of the cooling rate

! After first pass, skip following entry of
! temperatures and cooling rates
! If LE=1, then rate in deg/year
! If LE=0, then depth in slab in km
! If LE=-1 then characteristic rate 1/yr

IF (II*JJ.EQ.1) THEN

READ (4,*) (TFINALS(K),K=1,NT) !Final T must be neg
! or else years to cool

WRITE (5,*)"TFINAL (K) or years to cool if positive '

WRITE(5,*) (TFINALS(K),K=1,NT)

READ (4,*) (RATES(K),K=1,NR)

WRITE (5,*)"RATE (K/a) or depth or characteristic rate'

WRITE(5,*) (RATES(K),K=1,NR)

ENDIF

WRITE (5,*)" '

PRINT*, 'File COOLDA2 has been read; calculations underway'

! Now set the final temperature TFINAL and RATE

TIME=0.

NTF=II

TFINAL=TFINALS(II)

RATE=RATES(JJ)

TEMP=TEMPTLE(TZERO,RATE,TIME,LE,TSURF)

NSTEPS=NMAX

C Calculate concentrations using starting temp TZERO

C and a polynomial fit to wt % Al₂O₃ as f(T) at

C 20 kb based on values calculated with Harley (1984)

C for the compositions in garnet 1 of GR 1

C C(1) = -0.617931 for 18 kb

C C(2) = 1.25765 for 18 kb

C C(3) = -0.894610 for 18 kb

C C(4) = 1.69128 for 18 kb

C(1) = -0.376626 !C's are fit as f(T/1000)

C(2) = 0.637697 !they are polynomial coefficients

C(3) = -0.568287 ! these are fit for 1373 to 873K

C(4) = 1.46932 ! at 20 kb

T4 = TZERO/1000.0

WPCTAL = C(1)+T4*(C(2)+T4*(C(3)+T4*C(4)))

! Initialize the concentrations

DO (I=1,NX)

U(I)=WPCTAL

REPEAT

C Part omitted here for reiterative loop (st 90 etc)

```

TOTALT=TFINAL
IF (TOTALT.LT.0.0) THEN
  TFINAL = - TOTALT
  IF (LE.LT.0) TOTALT=ALOG(TEMP/TFINAL)/RATE
  IF (LE.EQ.0) TOTALT=TOTERF(TZERO,RATE,TSURF,TFINAL)
  IF (LE.GT.0) TOTALT=(TEMP-TFINAL)/RATE
ELSE IF (TOTALT.GE.0.0) THEN
  TFINAL=TEMPTLE(TEMP,RATE,TOTALT,LE,TSURF)
END IF

WRITE(5,*)"Start at T(K) ',TZERO,' end at ',TFINAL
IF (LE.EQ.1) WRITE(5,*) 'linear cooling rate'
IF (LE.EQ.-1) WRITE(5,*) 'exponential cooling',
* ' and "rate" is characteristic value'
* IF (LE.EQ.0) WRITE(5,*) '"rate" is depth in km',
* ' and cooling slab model was used'
WRITE(5,*)"Time required ',TOTALT,' at rate ',RATE
WRITE(5,*)"Initial wt % Al2O3, WPCTAL, was ',WPCTAL

```

C Choose DT value

C DDT is the diffusivity in microns²/year multiplied by DTMIN.
C The time increment (DT) is never allowed to exceed DTMAX.
C DT begins at DTMIN but it is scaled up by a factor of the
C ratio (D at T initial)/(D at last T) at the end of each loop.

```

DSTART=DZERO*EXP(-H/(RGAS*TEMP))
WRITE(5,*)"Initial D (microns2/yr) is ',DSTART
WRITE(5,*)"Initial D (meters2/sec) is ',DSTART/CONVERT

DDT=DTMIN*DZERO*EXP(-H/(RGAS*TEMP)) !not exceeded
DT=DTMIN

TIME=TIME+DT

```

C Step through time

```

DO (I=1,NSTEPS)
  OLDEMP = TEMP
  TEMP = TEMPTLE(TZERO,RATE,TIME,LE,TSURF)

```

```
IF (TEMP.LT.TFINAL) EXIT !Beware - an extension to F77
```

```

D = DZERO*EXP(-H/(RGAS*TEMP))
OLDCO = WPCTAL
T4 = TEMP/1000.0 ! For Harley opx composition
WPCTAL = C(1)+T4*(C(2)+T4*(C(3)+T4*C(4)))
UNEW(NX) = WPCTAL !at boundary with garnet
U(NX) = UNEW(NX)
CALL TSTEP (U,UNEW,DX,DT,D,NX,OLDCO)
DO (J = 1,NX-1)
  U(J) = UNEW(J)
REPEAT
OLDSTEP = DT !preserved for output at end
TIME = TIME + DT

```

```

TOTALT = TOTALT - DT
IF (TOTALT.GT.0.) THEN
    DT = DDT/D !lengthens step as D decreases
    IF (DT.GT.DTMAX) DT = DTMAX!limits max time
    IF (DT.GT.TOTALT) DT = TOTALT! finish
ENDIF

REPEAT

WRITE (5,*) I-1,' Steps',TIME,' years'
WRITE (5,*) 'First time step (yrs) was ',DTMIN,
1   ' and last step was ',OLDSTEP

C Hold at the current temperature for HOLDTIM
C for 100 steps
IF (HOLDTIM.EQ.0.) GO TO 220
TLEFT = HOLDTIM
IF (HOLDTIM.LT.0.) TLEFT=-HOLDTIM-TIME
IF (TLEFT.LT.0.) GO TO 220
TOTALT = TLEFT
DT = TLEFT/100.
NHOLD = 100
DO (I=1,NHOLD)
    CALL TSTEP (U,UNEW,DX,DT,D,NX,OLDCO)
    DO (J=1,NX-1)
        U(J) = UNEW(J)
    REPEAT
    TIME = TIME + DT
    TOTALT = TOTALT - DT
    IF (TOTALT.LE.0.) GO TO 220
REPEAT
WRITE (5,*) NHOLD,' steps',TLEFT,' years'
C End of holding period
220  CONTINUE

WRITE (5,*) 'Elapsed TIME ',TIME,' Final T ', OLDEMP
WRITE (5,*)'Final wt % Al2O3 at contact ',WPCTAL
WRITE (5,*) 'D at final temp (microns2/yr)',D
WRITE (5,*) 'D at final temp (meters2/sec)',D/CONVERT
WRITE (5,*) '
WRITE (5,*) 'Wt % Al2O3 in en'
WRITE (5,330) (UNEW(J),J=1,NX)

DO (J=1,NX)
    WRITE(6,340) X(J),UNEW(J)
REPEAT

240  CONTINUE ! end of loop DO 240 II=1,NT
    ! for multiple final temps and rates (not tested)

330  FORMAT (5(F12.4,2X))
340  FORMAT (F12.4,F12.4)

CALL TIME(SECONDS)
WRITE(5,*)'Seconds for execution = ',SECONDS-STARTTIME

PRINT*, 'Output to files COOLOU and COOLPL'

```

```
Print*,'Press RETURN to exit this program'
```

```
CLOSE(UNIT=5)
CLOSE(UNIT=6)
PAUSE
```

```
END
```

SUBROUTINE THOMAS (A,B,C,U,D,N)

```
C Solve a tridiagonal system by the Thomas method, overwriting
C arrays B and D. Arrays A, B, C are the lower, middle, upper
C diagonals, U is the unknown, and D is the right hand
C side of the equation.
```

```
REAL A(N), B(N), C(N), U(N), D(N)
DO (I=2,N-1)
    XMULT=A(I)/B(I-1)
    B(I)=B(I)-XMULT*C(I-1)
    D(I)=D(I)-XMULT*D(I-1)
REPEAT
U(N-1)=D(N-1)/B(N-1)
DO (I=2,N-1)
    U(N-I)=(D(N-I)-C(N-I)*U(N-I+1))/B(N-I)
REPEAT
RETURN
END
```

SUBROUTINE TRIAG (QA,QB,QC,UOLD,N,OLDCO)

```
REAL QA(N), QB(N), QC(N), UOLD(N), TEMP(1000)
```

```
DO (I=1,1000)
    TEMP(I)=0.0
REPEAT
```

```
TEMP(1) = QB(1)*UOLD(1) + QC(1)*UOLD(2)
TEMP(N-1) = QA(N-1)*UOLD(N-2) + QB(N-1)*UOLD(N-1) +
1 (1.0 + (1.0/(N-1)))*UOLD(N) + (1.0+(1.0/(N-1)))*OLDCO
DO (I=1,N-3)
    TEMP(I+1) = QA(I+1)*UOLD(I) + QB(I+1)*UOLD(I+1)
    + QC(I+1)*UOLD(I+2)
REPEAT
DO (I=1,N-1)
    UOLD(I)=TEMP(I)
REPEAT
RETURN
END
```

SUBROUTINE TSTEP (UOLD,UNEW,DX,DT,D,N,OLDCO)

```
C Advance the concentration vector one time step
C by first computing the P matrix, and then solving
C the equation P*UNEW=UOLD for UNEW by the Thomas
C tridiagonal method.
```

```
C N is the number of points in the concentration vector
C D is the current diffusivity value
```

```
REAL PA(1000),PB(1000),PC(1000),QA(1000),QB(1000),QC(1000)
REAL UOLD(N), UNEW(N)
CALL RCRANK (QA,QB,QC,PA,PB,PC,N,D,DX,DT)
CALL TRIAG (QA,QB,QC,UOLD,N,OLDCO)
```

```
C Now solve the simultaneous equations
```

```
CALL THOMAS (PA,PB,PC,UNEW,UOLD,N)
```

```

RETURN
END

SUBROUTINE RCRANK (QA,QB,QC,PA,PB,PC,N,D,DX,DT)
C Radial Crank-Nicholson solution
REAL PA(N), PB(N), PC(N), QA(N), QB(N), QC(N)
REAL CONST1,CONST2,APLUS,AMINUS,B
C=2.0*DX*DX/(D*DT)
PA(1) = 0.0
QA(1) = 0.0
PB(1) = C + 2.0
QB(1) = C - 2.0
PC(1) = -2.0
QC(1) = 2.0
I1 = 2
C Point I1, to just before the next point I2
I2 = N-2
DO (I=I1,I2)
    PA(I) = 1.0/I - 1.0
    PB(I) = C + 2.0
    PC(I) = -1.0/I - 1.0
    QA(I) = 1.0 - (1.0/I)
    QB(I) = C-2.0
    QC(I) = 1.0 + (1.0/I)
REPEAT
C Do the point at the boundary
PA(N-1) = -1.0 + (1.0/(N-1))
QA(N-1) = 1.0 - (1.0/(N-1))
PB(N-1) = C + 2.0
QB(N-1) = C - 2.0
PC(N-1) = 0.0
QC(N-1) = 0.0
RETURN
END

FUNCTION TOTERF (TZERO,RATE,TSURF,TFINAL)
! Compute total time for conductive cooling to TFINAL
! Rate is depth in km when LE = 0

TLOW = 0.0
TU = 4.0E9 !Search over a 4 Ga interval
T1 = TLOW
DO (J=1,10)
    DT = (TU-TLOW)/10. !search increment
    DO (I=1,10)
        TIME = I*DT + TLOW
        TEMP2 = TEMPTLE(TZERO,RATE,TIME,0,TSURF)
        IF (TEMP2.LE.TFINAL) EXIT
        T1 = TIME
    REPEAT
    TU = TIME !now reset the interval to be searched
    TLOW = T1
REPEAT
TOTERF = TU
RETURN
END

FUNCTION TEMPTLE (TZERO,RATE,TIME,LE,TSURF)

```

! Compute temperature TEMPTLE at TIME for initial
 ! value TZERO for a linear decrease (LE = 1),
 ! or an exponential decrease (LE=-1), or a cooling
 ! slab model (LE = 0). For the cooling slab model,
 ! the rate is the depth in the slab in km and the
 ! thermal diffusivity is appropriate for the mantle.

```

IF (TIME.EQ.0.) THEN
  TEMPTLE = TZERO !avoids dividing by 0 below
ELSE IF (LE.EQ.-1) THEN
  TEMPTLE=TZERO*EXP(-RATE*TIME)
ELSE IF (LE.EQ.0) THEN
  TEMPTLE=(TZERO-TSURF)*
  ERF(.5*RATE/SQRT(2.641E-5*TIME))+TSURF
1 ELSE IF (LE.EQ.1) THEN
  TEMPTLE=TZERO-RATE*TIME
END IF
RETURN
END
  
```

```

FUNCTION ERF(X) !Press et al., 1989, Numerical Recipes, p 164
!Returns erf(x) to a fractional error < 1.2e-7
Z = ABS(X)
T = 1./(1. + 0.5*Z)
ERFCC=T*EXP(-Z*Z-1.26551223+T*(1.00002368 +
* T*.37409196+T*(.09678418+T*(-.18628806 +
* T*(.27886807+T*(-1.13520398+T*(1.48851587 +
* T*(-.82215223+T*.17087277)))))))
IF (X.LT.0.) ERFCC = 2. - ERFCC
ERF = 1 - ERFCC
RETURN
END
  
```

```
75
3.0
3.8
500000.0
1800
100000
4000000
1373
1
1
0
-973.
0.000001
```

The input file, COOLDA2, is above. An annotated version is below.

75	NX, number of x increments
3.0	DX, x increment in micrometers
3.8	DZERO, pre-exponential coefficient for D
500000.0	H, activation enthalpy for D
1800	NMAX, maximum limit of time steps
100000	DTMIN, minimum time step
4000000	DTMAX, maximum time step
1373	TZERO, starting T in degrees K
1	NT, number of final temperatures
1	LE, 1 is linear
0	HOLDTM, years to hold (if positive)
-973.	TFINAL, negative of desired final T (K)
0.000001	RATE, deg/yr (or characteristic rate or depth)

One of the output files "COOLOU" from Smith-Barron program

05/01/91 D Smith COOLV3 Harley, 6/15/90 for gar 1, GR1, 20 kb
NX is 75 DX is 3.00000
DZERO in meters²/sec is 3.80000
H, Activation Q for diffusion (joules) 500000.
NMAX number of time steps = 1800
DTMIN = 100000. DTMAX = 4.000000E+06 YRS
TZERO starting T(deg K) 1373.00 at PRESSR P(bars) 20000.0
Number of final temps is 1
1, linear: 0, slab: -1, exp: LE = 1
HOLDTIM (if -, cooling + holding) .000000
TFINAL (K) or years to cool if positive
-973.000
RATE (K/a) or depth or characteristic rate
1.000000E-06

Start at T(K) 1373.00 end at 973.000
linear cooling rate
Time required 4.000000E+08 at rate 1.000000E-06
Initial wt % Al₂O₃, WPCTAL, was 3.23065
Initial D (microns²/yr) is 11.3794
Initial D (meters²/sec) is 3.605908E-19
372 Steps 4.000988E+08 years
First time step (yrs) was 100000. and last step was 1.610304E+06
Elapsed TIME 4.000988E+08 Final T 974.512
Final wt % Al₂O₃ at contact 1.06494
D at final temp (microns²/yr) 1.894517E-07
D at final temp (meters²/sec) 6.003363E-27

Wt % Al₂O₃ in en

1.6527	1.6526	1.6525	1.6524	1.6522
1.6519	1.6516	1.6512	1.6508	1.6504
1.6499	1.6493	1.6487	1.6481	1.6474
1.6466	1.6458	1.6450	1.6440	1.6431
1.6420	1.6409	1.6398	1.6386	1.6373
1.6359	1.6345	1.6330	1.6315	1.6298
1.6281	1.6263	1.6244	1.6225	1.6204
1.6183	1.6160	1.6137	1.6112	1.6086
1.6059	1.6031	1.6001	1.5970	1.5938
1.5904	1.5868	1.5830	1.5791	1.5749
1.5705	1.5659	1.5610	1.5558	1.5503
1.5444	1.5382	1.5315	1.5244	1.5167
1.5084	1.4994	1.4896	1.4789	1.4670
1.4538	1.4390	1.4222	1.4027	1.3796
1.3516	1.3163	1.2687	1.1980	1.0649

Seconds for execution = 32.0000

Representative electron probe analyses - Smith and Barron

PHN 4803 Representative compositions for P-T calculations										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum		Data of Mar 21, 1989
57.3	0.00	0.86	0.28	4.86	36.0	0.23	0.05	99.6		Opx
54.4	0.00	2.32	1.44	1.69	16.4	21.3	1.54	99.1		Cpx
42.1	0.00	21.7	2.56	8.25	20.2	4.99	0.00	99.8		Garnet
J34 Representative compositions for P-T calculations										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum		Data of June 15, 1990
58.3	0.00	0.75	0.22	4.73	35.8	0.22	0.04	100.1		Opx
54.5	0.02	2.36	1.73	1.84	15.8	21.3	1.77	99.3		Cpx
42.2	0.00	21.4	2.65	8.17	20.1	4.90	0.00	99.4		Garnet
42.3	0.00	0.00	0.00	7.70	51.7	0.02	0.00	101.7		Olivine
Garnet 10, GR1 Representative compositions for P-T calculations										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum		Data of Dec 12, 1986
54.4	0.16	2.06	0.93	1.38	16.4	22.6	1.19	99.1		Cpx 2.8 μm from contact
42.1	0.04	22.1	1.85	8.79	19.3	5.18	0.02	99.4		Gar 2.8 μm from contact
										Data of Oct 31, 1986
41.6	0.00	0.00	0.00	6.29	51.4	0.02	0.00	99.3		Olivine
41.8	0.08	22.2	1.99	8.59	19.3	5.49	0.00	99.5		Nearby Garnet
Garnet 1, GR1 Representative compositions for P-T calculations										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum		Data of Oct 17, 1986
58.0	0.05	1.06	0.29	3.83	36.6	0.14	0.00	100.0		Opx 2.8 μm from contact
42.2	0.04	22.0	1.71	8.10	19.1	5.50	0.00	98.7		Gar 2.8 μm from contact
										Data of Nov 10, 1986
41.5	0.00	0.00	0.00	5.62	52.4	0.00	0.00	99.5		Olivine
42.3	0.09	22.8	1.73	7.86	20.4	5.25	0.02	100.6		Nearby Garnet
Pr35 Representative compositions for P-T calculations										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum		Data of Apr 4, 1990
56.7	0.02	0.75	0.06	14.0	30.0	0.11	0.00	101.6		Opx
54.9	0.14	3.71	0.32	4.47	14.1	20.9	2.24	100.8		Cpx
40.2	0.02	22.7	0.41	21.9	10.7	5.08	0.00	101.0		Garnet
Prs90q Representative compositions for P-T calculations										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum		Data of Apr 24, 1990
56.9	0.00	1.10	0.16	9.08	33.2	0.14	0.00	100.6		Opx
54.1	0.23	5.28	0.88	2.57	14.0	21.2	1.77	100.1		Cpx
41.2	0.02	23.0	0.70	16.1	14.5	5.10	0.02	100.7		Garnet

Representative electron probe analyses - Smith and Barron

Garnet-orthopyroxene traverse Garnet 1, GR1 Navajo field (Garnet Ridge)											
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum	μm	from contact	
41.8	0.07	21.7	1.74	7.88	19.5	5.44	0.02	98.1	18.4	start of traverse	
42.6	0.06	21.9	1.74	7.93	19.7	5.49	0.00	99.4	17.0	Garnet 1 GR 1	
41.7	0.07	21.8	1.74	7.87	19.4	5.55	0.00	98.1	15.6	Data of Oct 17, 1986	
42.4	0.07	22.0	1.76	7.90	19.4	5.57	0.00	99.2	14.1		
41.8	0.06	21.7	1.74	7.91	19.4	5.40	0.00	98.0	12.7	On about the same	
42.9	0.07	21.8	1.70	8.02	19.5	5.48	0.02	99.4	11.3	diameter as the	
41.9	0.05	21.6	1.72	8.05	19.4	5.47	0.02	98.3	9.9	traverse of 6/30/82	
42.5	0.06	21.8	1.72	7.98	19.5	5.46	0.02	98.9	8.5		
41.7	0.05	21.8	1.74	8.11	19.3	5.61	0.00	98.3	7.1		
42.5	0.05	21.9	1.68	8.06	19.3	5.42	0.00	98.9	5.7		
41.9	0.05	21.6	1.73	8.06	19.1	5.49	0.00	98.0	4.2		
42.2	0.04	22.0	1.71	8.10	19.1	5.50	0.00	98.7	2.8		
42.1	0.03	21.5	1.75	8.30	19.6	5.42	0.00	98.8	1.4		
48.3	0.03	17.2	1.24	7.20	25.8	4.19	0.02	103.9	0.0	taken as contact	
57.3	0.04	1.11	0.27	3.80	36.0	0.17	0.00	98.6	1.4		
58.0	0.05	1.06	0.29	3.83	36.6	0.14	0.00	100.0	2.8		
57.3	0.06	1.13	0.30	3.79	36.2	0.16	0.00	98.9	4.2		
58.0	0.07	1.17	0.31	3.75	36.3	0.19	0.02	99.8	5.7		
57.2	0.08	1.23	0.31	3.92	36.1	0.19	0.02	99.1	7.1		
58.0	0.07	1.22	0.32	3.83	36.1	0.17	0.00	99.7	8.5		
57.2	0.08	1.24	0.30	3.92	35.6	0.18	0.00	98.5	9.9		
57.8	0.08	1.27	0.30	3.81	36.0	0.20	0.02	99.5	11.3		
57.1	0.09	1.27	0.33	3.91	36.0	0.21	0.02	98.9	12.7		
57.8	0.09	1.31	0.33	3.97	36.1	0.20	0.02	99.8	14.1		
57.1	0.09	1.31	0.33	3.85	35.7	0.20	0.02	98.6	15.6		
57.6	0.09	1.33	0.34	3.89	35.7	0.22	0.00	99.2	17.0		
57.1	0.09	1.31	0.34	3.96	35.8	0.22	0.02	98.9	18.4		
57.2	0.09	1.36	0.34	3.99	36.0	0.21	0.02	99.2	19.8	end of traverse	
57.2	0.11	1.65	0.39	4.17	35.5	0.27	0.02	99.3	159	central opx	

Representative electron probe analyses - Smith and Barron

Traverse for 3 elements only across diameter of opx inclusion in Garnet 1, GR1. Data of 6/30/82										
K-values for these data were collected on a 3-spectrometer ARL probe (all other data collected on JEOL)										
Correction factors by reference to complete analyses on 10/17/86: Al ₂ O ₃ (original estimate)*1.65/1.74										
d (μm)	r (μm)	CaO	FeO	Al ₂ O ₃	d (μm)	r (μm)	CaO	FeO	Al ₂ O ₃	
4	222	0.17	3.90	1.19	235	12	0.34	4.21	1.66	d is the original traverse
7	219	0.19	3.95	1.28	247	24	0.35	4.25	1.65	distance
10	216	0.18	3.96	1.31	259	36	0.32	4.32	1.69	r is the radial distance
13	213	0.20	4.02	1.34	271	48	0.32	4.30	1.71	from the center
16	210	0.21	4.05	1.37	283	60	0.33	4.23	1.65	
19	207	0.22	4.07	1.40	295	72	0.33	4.30	1.66	
22	204	0.23	4.08	1.39	307	84	0.32	4.27	1.63	
25	201	0.24	4.05	1.42	319	96	0.32	4.23	1.65	
28	198	0.23	4.09	1.43	331	108	0.32	4.31	1.61	
31	195	0.23	4.11	1.46	343	120	0.32	4.30	1.64	
34	192	0.24	4.08	1.47	355	132	0.32	4.23	1.57	
37	189	0.25	4.07	1.45	361	138	0.30	4.25	1.57	
40	186	0.26	4.18	1.48	367	144	0.32	4.23	1.60	
43	183	0.27	4.13	1.48	373	150	0.31	4.22	1.59	
46	180	0.27	4.16	1.47	379	156	0.30	4.26	1.60	
49	177	0.27	4.17	1.47	385	162	0.31	4.27	1.55	
52	174	0.27	4.15	1.49	391	168	0.29	4.22	1.54	
55	171	0.28	4.17	1.48	397	174	0.30	4.27	1.55	
58	168	0.29	4.18	1.49	400	177	0.28	4.27	1.53	
61	165	0.28	4.15	1.53	403	180	0.29	4.25	1.56	
64	162	0.28	4.15	1.51	406	183	0.30	4.23	1.52	
67	159	0.30	4.11	1.50	409	186	0.28	4.24	1.50	
73	153	0.28	4.19	1.52	412	189	0.28	4.25	1.47	
79	147	0.31	4.15	1.54	415	192	0.28	4.17	1.48	
85	141	0.30	4.14	1.58	418	195	0.27	4.20	1.47	
91	135	0.30	4.18	1.55	421	198	0.27	4.19	1.49	
97	129	0.32	4.20	1.57	424	201	0.26	4.18	1.47	
103	123	0.30	4.18	1.58	427	204	0.24	4.13	1.47	
109	117	0.31	4.23	1.56	430	207	0.24	4.13	1.45	
115	111	0.31	4.23	1.62	433	210	0.21	4.20	1.43	
121	105	0.32	4.20	1.59	436	213	0.22	4.13	1.41	
127	99	0.32	4.22	1.61	439	216	0.20	4.08	1.35	
139	87	0.32	4.21	1.62	442	219	0.20	4.06	1.33	
151	75	0.32	4.24	1.58	445	222	0.18	3.99	1.23	
163	63	0.32	4.20	1.61						
175	51	0.32	4.22	1.65						
187	39	0.34	4.21	1.62						
199	27	0.34	4.29	1.65						
211	15	0.34	4.22	1.63						
223	3	0.33	4.25	1.65						
223	0	0.33	4.25	1.65						

Representative electron probe analyses - Smith and Barron

Garnet-Clinopyroxene traverse, Garnet 10, GR 1, Navajo field (Garnet Ridge)										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum	μm	from garnet contact
47.7	0.06	17.3	1.34	6.84	18.6	9.3	0.24	101.4	0	Contact
53.6	0.13	2.59	0.79	1.52	16.7	22.5	1.09	99.0	1.4	Garnet 10, GR 1
54.5	0.17	2.17	0.90	1.37	16.3	22.7	1.20	99.3	2.8	Data of Dec 12, 1986
53.2	0.18	2.21	1.00	1.42	16.2	22.4	1.21	97.9	4.2	Clinopyroxene
54.3	0.20	2.31	1.04	1.40	16.1	22.5	1.27	99.1	5.7	
53.5	0.19	2.32	1.04	1.44	16.2	22.5	1.28	98.5	7.1	
54.3	0.20	2.40	1.08	1.44	16.0	22.4	1.33	99.1	8.5	
53.9	0.20	2.44	1.12	1.51	16.3	22.4	1.31	99.0	9.9	
54.7	0.20	2.48	1.14	1.47	16.1	22.3	1.38	99.8	11.3	
53.6	0.19	2.49	1.16	1.51	16.3	22.4	1.35	98.9	12.7	
54.4	0.20	2.50	1.15	1.51	16.0	22.3	1.41	99.6	14.1	
53.7	0.21	2.55	1.18	1.51	16.2	22.5	1.41	99.2	16.3	
54.5	0.21	2.56	1.18	1.52	16.1	22.4	1.42	99.8	19.8	
53.8	0.22	2.59	1.24	1.44	16.1	22.5	1.40	99.3	22.6	
54.4	0.20	2.63	1.20	1.46	16.1	22.4	1.44	99.8	25.5	
53.4	0.21	2.65	1.22	1.43	16.1	22.4	1.43	98.8	28.3	
54.2	0.20	2.76	1.25	1.49	16.0	22.4	1.49	99.8	33.9	
53.4	0.20	2.80	1.27	1.51	16.0	22.3	1.51	99.0	39.6	
54.5	0.21	2.87	1.26	1.50	16.0	22.3	1.51	100.1	45.3	
53.9	0.19	2.92	1.25	1.55	16.0	22.2	1.55	99.5	50.9	
54.9	0.20	3.00	1.28	1.54	15.8	22.0	1.56	100.3	62.2	
53.9	0.20	3.06	1.28	1.52	16.0	22.1	1.53	99.6	73.5	
54.5	0.20	3.11	1.30	1.46	16.0	21.9	1.55	99.9	84.9	
53.7	0.20	3.20	1.30	1.50	15.9	22.4	1.60	99.7	96.2	
55.0	0.20	3.26	1.27	1.43	15.7	22.2	1.59	100.6	107	
53.8	0.20	3.01	1.25	1.65	17.0	20.7	1.49	99.1	119	
54.5	0.21	3.34	1.29	1.48	15.7	22.4	1.63	100.4	130	
53.5	0.20	3.34	1.31	1.50	15.8	22.0	1.62	99.2	141	one end of traverse
Garnet-Clinopyroxene traverse, Garnet 10, GR 1, Navajo field (Garnet Ridge)										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum	μm	from Cpx contact
49.0	0.06	15.7	1.25	6.30	18.6	10.6	0.33	101.8	0	contact
43.0	0.04	22.3	1.76	8.61	19.6	5.26	0.00	100.5	1.4	Garnet 10 GR 1
42.1	0.04	22.1	1.85	8.79	19.3	5.18	0.02	99.4	2.8	Data of Dec 12, 1986
42.8	0.05	22.1	1.89	8.73	19.7	5.11	0.00	100.4	4.2	Garnet
42.1	0.05	22.0	1.92	8.76	19.5	5.19	0.00	99.5	5.7	
42.8	0.05	22.1	1.93	8.73	19.6	5.22	0.02	100.5	7.1	
42.3	0.05	22.0	1.95	8.70	19.5	5.11	0.00	99.6	8.5	
42.7	0.05	22.1	1.98	8.65	19.6	5.22	0.02	100.3	9.9	
42.5	0.05	21.8	1.98	8.70	19.5	5.11	0.02	99.6	11.3	
42.8	0.05	22.1	1.99	8.73	19.7	5.07	0.00	100.4	12.7	
42.0	0.05	21.7	2.00	8.70	19.4	5.07	0.02	98.9	14.1	
42.7	0.06	21.9	2.04	8.72	19.7	5.16	0.02	100.3	15.6	
42.4	0.06	21.9	2.01	8.76	19.4	5.11	0.00	99.6	17.0	
42.5	0.05	22.0	2.05	8.77	19.7	5.16	0.02	100.2	18.4	
42.0	0.06	21.7	2.03	8.63	19.4	5.11	0.02	99.0	19.8	
42.8	0.06	21.8	2.06	8.75	19.7	5.08	0.02	100.3	21.2	

Representative electron probe analyses - Smith and Barron

42.3	0.06	21.6	2.07	8.65	19.4	5.07	0.02	99.2	22.6	
42.7	0.06	21.9	2.06	8.74	19.5	5.08	0.02	100.1	24.0	continuation of 12/12/86
41.9	0.06	21.6	2.09	8.72	19.4	5.21	0.02	99.0	25.5	traverse Garnet 10 GR1
42.8	0.06	21.9	2.08	8.68	19.7	5.15	0.02	100.4	26.9	
42.1	0.06	21.7	2.07	8.74	19.5	5.10	0.02	99.3	28.3	
42.8	0.06	21.8	2.09	8.66	19.5	5.16	0.02	100.1	29.7	
42.2	0.06	21.6	2.10	8.75	19.5	5.16	0.02	99.4	38.2	
42.5	0.06	21.8	2.12	8.69	19.5	5.26	0.02	99.9	46.7	
42.2	0.07	21.6	2.12	8.74	19.5	5.27	0.02	99.6	55.2	
42.8	0.07	21.7	2.12	8.67	19.6	5.29	0.02	100.2	63.6	
42.2	0.07	21.6	2.11	8.71	19.5	5.29	0.02	99.5	72.1	
42.4	0.07	21.7	2.13	8.75	19.6	5.27	0.02	100.0	80.6	
42.3	0.07	21.5	2.12	8.69	19.4	5.24	0.03	99.4	89.1	
42.7	0.07	21.6	2.13	8.72	19.5	5.27	0.02	100.0	97.6	
42.1	0.07	21.5	2.13	8.69	19.4	5.24	0.02	99.1	106	
42.7	0.07	21.9	2.17	8.72	19.6	5.34	0.02	100.5	115	
41.8	0.08	21.4	2.14	8.67	19.2	5.23	0.02	98.5	132	
42.8	0.07	21.6	2.13	8.69	19.5	5.32	0.03	100.2	149	other end of traverse
42.0	0.05	21.6	1.98	8.60	19.3	5.04	0.02	98.6	14	repeat a point
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum	μm	from Cpx contact

Representative electron probe analyses - Smith and Barron

Pr35 websterite Chino Valley, AZ traverses across opx-gar-cpx lamellae											
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum	μm	Pr35	
40.88	0.01	22.69	0.41	21.58	10.82	5.34	0.00	101.73	0	start	
40.24	0.02	22.72	0.41	21.86	10.71	5.08	0.00	101.03	5	Data of 4/4/90	
56.68	0.02	0.75	0.06	13.97	30.01	0.11	0.00	101.59	10		
56.11	0.01	0.85	0.08	13.87	29.85	0.13	0.00	100.91	13		
56.52	0.01	1.05	0.10	13.96	29.41	0.12	0.00	101.17	16		
55.66	0.00	1.14	0.10	14.01	29.51	0.12	0.02	100.55	19		
56.37	0.00	1.23	0.10	14.01	29.39	0.13	0.02	101.24	22		
55.14	0.02	1.40	0.10	13.83	28.96	0.41	0.03	99.89	25		
55.92	0.01	1.30	0.11	14.12	29.26	0.14	0.02	100.88	28		
55.87	0.01	1.36	0.11	14.08	29.15	0.14	0.00	100.72	31		
56.57	0.00	1.25	0.11	13.93	29.21	0.13	0.07	101.26	34		
56.17	0.00	1.05	0.10	13.93	29.35	0.10	0.02	100.72	37		
56.84	0.00	0.81	0.08	13.98	29.33	0.13	0.00	101.17	40		
55.94	0.00	1.03	0.09	13.88	29.57	0.12	0.00	100.62	45		
56.71	0.02	1.09	0.10	13.85	29.61	0.12	0.03	101.53	50		
48.43	0.27	11.50	0.43	8.08	19.74	11.14	0.48	100.07	55	amphibole? and crack	
57.09	0.01	0.55	0.06	13.33	29.95	0.12	0.03	101.13	60		
55.92	0.04	0.72	0.05	14.37	29.20	0.17	0.02	100.48	65		
49.19	0.10	14.50	0.31	18.08	20.34	2.42	0.08	105.00	68		
43.34	0.04	23.81	0.29	11.42	8.94	8.51	0.23	96.59	71		
40.65	0.05	22.75	0.37	22.73	10.24	4.82	0.00	101.61	74	end	
55.89	0.03	1.33	0.09	14.23	29.26	0.17	0.02	101.01	0	start	
55.70	0.02	1.15	0.10	13.96	29.43	0.22	0.00	100.56	5		
55.84	0.02	1.03	0.08	13.74	29.52	0.23	0.00	100.46	10		
40.34	0.05	22.50	0.35	21.94	10.84	4.97	0.00	101.00	15		
42.05	0.02	23.18	0.40	15.06	11.45	8.52	0.08	100.76	21		
55.85	0.03	1.12	0.08	13.91	29.75	0.22	0.02	100.98	25		
55.77	0.03	1.36	0.10	14.16	29.28	0.17	0.03	100.90	30		
55.23	0.04	1.27	0.09	13.94	29.02	0.25	0.02	99.86	35		
56.01	0.04	1.35	0.08	14.17	28.97	0.22	0.02	100.87	40		
55.34	0.07	1.65	0.09	14.23	29.52	0.22	0.02	101.13	45		
55.68	0.07	1.13	0.08	14.02	29.12	0.23	0.02	100.34	50		
54.87	0.14	3.71	0.32	4.47	14.13	20.89	2.24	100.77	55		
54.66	0.14	3.63	0.31	4.39	14.03	20.89	2.17	100.21	60		
54.52	0.11	3.56	0.31	4.27	14.24	21.02	2.20	100.22	65		
54.71	0.12	3.53	0.31	4.29	14.00	20.97	2.14	100.07	70	end	
54.80	0.02	1.15	0.10	14.20	29.18	0.18	0.02	99.66	0	start	
54.87	0.03	0.83	0.06	13.95	29.37	0.19	0.02	99.31	3		
40.08	0.00	21.16	0.44	20.57	12.33	4.85	0.00	99.43	6		
53.86	0.02	3.16	0.09	14.60	28.29	0.76	0.00	100.78	9		
55.22	0.02	1.00	0.09	14.06	29.43	0.17	0.02	100.01	12		
54.99	0.02	1.13	0.09	14.08	29.31	0.17	0.02	99.80	15		
54.41	0.02	1.22	0.09	14.06	29.20	0.19	0.02	99.19	18		
55.37	0.03	1.25	0.10	13.99	29.39	0.16	0.02	100.31	21		
54.56	0.02	1.24	0.09	13.87	28.92	0.21	0.02	98.93	24	end	

Representative electron probe analyses - Smith and Barron

Prs90q, websterite xenolith, Chino Valley, AZ data of 4/24/90										
SiO ₂	TiO ₂	Al ₂ O ₃	Cr ₂ O ₃	FeO*	MgO	CaO	Na ₂ O	Sum	µm	Comments
56.47	0.01	2.49	0.44	9.53	32.0	0.12	0.00	101.05	20	C2 opx 20µm from garnet
54.86	0.03	5.80	0.60	9.84	30.1	0.16	0.03	101.44	105	opx interior
54.94	0.02	4.47	0.54	9.75	30.9	0.19	0.04	100.82	55	C4 back towards C2
56.34	0.02	3.75	0.48	9.72	31.1	0.18	0.02	101.61	44	same line
41.82	0.03	23.16	0.82	15.7	14.7	5.31	0.00	101.60		C1 adjacent garnet
41.78	0.02	23.06	0.74	16.2	14.8	5.05	0.00	101.62		C5 same gar by opx C2
41.91	0.01	22.94	0.86	16.2	14.5	5.33	0.00	101.72		C6 same gar near cpx
54.06	0.22	5.40	1.00	2.61	14.0	21.64	1.75	100.67	20	C7 cpx by garnet
53.74	0.38	7.50	1.00	2.73	13.0	21.16	1.96	101.47	48	into cpx interior on line
52.36	0.39	8.26	1.00	2.96	12.6	20.46	1.99	100.07	66	into cpx interior on line
52.26	0.42	8.40	0.97	3.12	12.6	21.10	1.68	100.60	118	into cpx interior on line
51.45	0.39	8.31	0.94	3.51	12.8	21.37	1.55	100.29	176	central cpx on line
41.76	0.02	23.19	0.60	16.1	14.8	5.06	0.02	101.52	25	gar - trav away from opx
41.04	0.01	23.15	0.61	16.1	14.8	5.14	0.02	100.87	30	gar - trav away from opx
41.72	0.00	23.29	0.64	16.1	14.7	5.18	0.03	101.69	35	gar - trav away from opx
41.50	0.02	23.09	0.61	16.0	14.8	5.24	0.02	101.23	40	gar - trav away from opx
41.45	0.01	23.33	0.59	16.1	14.7	5.33	0.03	101.49	45	gar - trav away from opx
41.05	0.02	23.00	0.70	16.2	14.8	4.94	0.02	100.64	15	gar - towards opx
41.56	0.02	23.13	0.76	16.5	14.7	4.99	0.00	101.60	10	gar - towards opx
41.28	0.00	22.97	0.76	16.5	14.6	5.01	0.02	101.13	5	gar - towards opx
49.64	0.06	17.82	0.35	9.87	16.3	6.49	0.54	101.03	0	gar-opx contact
56.92	0.00	1.10	0.16	9.08	33.2	0.14	0.00	100.58	5	opx - trav from contact
57.02	0.00	1.27	0.18	8.98	33.2	0.15	0.00	100.79	10	opx - trav from contact
56.68	0.01	1.31	0.20	8.94	33.0	0.15	0.00	100.23	15	opx - trav from contact
56.98	0.01	1.37	0.22	8.89	33.0	0.15	0.00	100.57	20	opx - trav from contact
57.66	0.01	1.37	0.23	9.04	32.7	0.13	0.00	101.14	25	opx - trav from contact
56.97	0.02	1.49	0.27	9.19	32.6	0.15	0.00	100.68	30	opx - trav from contact
56.38	0.01	1.53	0.27	9.14	32.5	0.16	0.00	99.94	35	opx - trav from contact
56.75	0.01	1.59	0.26	9.19	32.5	0.14	0.00	100.44	40	opx - trav from contact
56.40	0.00	1.60	0.27	9.16	32.4	0.14	0.00	99.92	45	opx - trav from contact
53.12	0.20	5.08	0.81	2.61	14.2	21.34	1.70	99.09		cpx in contact w opx
54.10	0.23	5.28	0.88	2.57	14.0	21.21	1.77	100.06		cpx in contact w gar